

## Homework



$$\Sigma \Delta P = 0$$

$$\Sigma P_i = \Sigma P_f$$

$$P_{Bi} - P_{Ri} = P_{BRf}$$

$$m_B v_{Bi} - m_R v_{Ri} = (m_B + m_R) v_f$$

$$(5 \text{ kg})(3 \text{ m/s}) - (2 \text{ kg})(4 \text{ m/s}) = (5 \text{ kg} + 2 \text{ kg}) v_f$$

$$7 \text{ kg m/s} = (7 \text{ kg}) v_f$$

$$v_f = 1 \text{ m/s}$$

## Collisions

During a collision momentum is transferred from one object to another.

During any event momentum is conserved, meaning:

- the amount of momentum at any time is the same

$$\sum P_i = \sum P_f$$

- there is no net change in the momentum of a system

$$\sum \Delta P = 0$$

## Impulse

- During a collision, momentum is transferred from one object to another. This changes the momentum for that object.
- Impulse is a measure of the change in momentum an object experiences. (Impulse equals change in momentum)

$$J = \Delta p$$

Like momentum, we find the mathematical definition for impulse from Newton's Second Law.

$$\Sigma F = ma = m \frac{\Delta v}{\Delta t}$$

$$\Sigma F = \frac{\Delta p}{\Delta t} \quad || \quad \frac{\Delta v}{\Delta t}$$

$$\Sigma F \Delta t = \Delta p = J$$

$$\begin{array}{ccc} \Sigma F \Delta t & = & m \Delta v \\ || & & || \\ J & = & \Delta p \end{array}$$

## Example

You apply a force of 5 N on an object for 3 seconds. What is the impulse? What is the object's change in momentum?

$$\begin{aligned} J &= \sum F \Delta t \\ &= (5\text{ N})(3\text{ s}) \\ &= 15\text{ N}\cdot\text{s} \end{aligned}$$

$$1\text{ N}\cdot\text{s} = 1\text{ kg}\cdot\text{m/s}$$

$$\begin{aligned} J &= \Delta p \\ \therefore \Delta p &= 15\text{ N}\cdot\text{s} \end{aligned}$$

A 200 g tennis ball, moving 25 m/s, is struck by a tennis player, causing the ball to move 30 m/s in the opposite direction. If the tennis racket makes contact with the ball for 0.65 s, what is the average force the tennis player exerts on the ball?

$$\begin{aligned} \sum F \Delta t &= m \Delta v & \Delta v &= v_f - v_i \\ & & &= 30\text{ m/s} - (-25\text{ m/s}) \\ & & &= 55\text{ m/s} \\ \sum F (0.65\text{ s}) &= (0.2\text{ kg})(55\text{ m/s}) & & \begin{array}{l} \longrightarrow \\ v_i = 25\text{ m/s} \\ \longleftarrow \\ v_f = 30\text{ m/s} \\ \text{"+"} \end{array} \\ \sum F &= \frac{11\text{ N}\cdot\text{s}}{0.65\text{ s}} \\ &= 16.9\text{ N} \end{aligned}$$

## The Conceptual Value of Impulse

Impulse is defined to be the change in momentum. The momentum of an object is changed when a net force is applied on an object over a period of time.

Varying the time an object experiences a force over affects the amount of force the object experiences for a given impulse.

## Conceptual Questions for Impulse

Why does it hurt less to fall on the grass than on the concrete?

Explain how a hammer can be used to push a nail into a board?

## Homework

Momentum/Impulse sheet. You can do all the questions now.